Original

**Examination:** 

Macroeconomic Analysis (No. 1428)

**Semester:** 

**Summer Semester 2003** 

**Examiner:** 

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The following aids may be used:

None.

## **Examination Questions:**

Consider a perfectly competitive economy with households, firms and a government. Households maximize

$$\int_{0}^{\infty} u[c(t),l(t),m(t)]e^{-\rho t} dt,$$

with

$$u(c,l,m) = \ln c - \alpha \ln l + \beta \ln m,$$

subject to a budget constraint

$$\dot{M} + \dot{B}_g + \dot{B}_f = i_g B_g + i_f B_f + Wl - Pc - T_h$$

when  $B_g$ ,  $B_f$  are nominal values of government and corporate bonds, respectively, held by the households;  $T_h$  denotes the nominal value of (lump-sum) taxes;  $\dot{M}$  is the change in nominal money balances (m=M/P).

The firms produce with an unchanging technology employing capital and labor, described by a Cobb-Douglas function. Their gross profit (revenue minus labor costs) is taxed at a constant tax rate  $0 < \tau < 1$ . They finance their investment by issuing corporate bonds, there are not any equity shares outstanding at t=0. Investment does not involve installation costs. Managers maximize the firms' value. At t=0 the capital stock is  $K(0)=K_0$ .



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The government budget constraint is

$$\dot{M} + \dot{B}_{g} = i_{g}B_{g} + Pg - T_{h} - T_{f}$$
,

where  $\dot{M}$  is the issue of (nominal) money, g is real government consumption, and  $T_f$  is nominal corporate tax revenue. Assume that the government's monetary policy implies a constant growth rate of M over the whole time period.  $T_h(t)$  is indexed to the price level P(t). The government starts with initial values  $M(0)=M_o$ ,  $B_g(0)=B_o>0$ .

- 1. Describe the dynamics of real capital and private consumption in a perfect foresight equilibrium.
- 2. How does the "consumption function" of the household sector look like if
  - a) the households are not aware of the government's intertemporal budget constraint?
  - b) they take the government's budget constraint into account?
- 3. Describe the stationary state of the economy in terms of model parameters and exogenous variables.
- 4. Analyse the consequences of an increase in
  - a) government consumption g,
  - b) the corporate tax rate  $\tau$ ,
  - c) the constant growth rate of M

for the stationary state (in particular the capital stock and real private consumption). Sketch graphically impact effects and adjustment paths.